# EUREKA MATH<sup>™</sup>

ABOUT EUREKA MATH	Created by the nonprofit Great Minds, <i>Eureka Math</i> helps teachers deliver unparalleled math instruction that provides students with a deep understanding and fluency in math. Crafted by teachers and math scholars, the curriculum carefully sequences the mathematical progressions to maximize coherence from Prekindergarten through Precalculus—a principle tested and proven to be essential in students' mastery of math.		
	Teachers and students using <i>Eureka Math</i> find the trademark "Aha!" moments in <i>Eureka Math</i> to be a source of joy and inspiration, lesson after lesson, year after year.		
ALIGNED	<i>Eureka Math</i> is the only curriculum found by EdReports.org to align fully with the Common Core State Standards for Mathematics for all grades, Kindergarten through Grade 8. Great Minds offers detailed analyses which demonstrate how each grade of <i>Eureka Math</i> aligns with specific state standards. Access these free alignment studies at greatminds.org/state-studies.		
DATA	Schools and districts nationwide are experiencing student growth and impressive test scores after using <i>Eureka Math</i> . See their stories and data at greatminds.org/data.		
FULL SUITE OF RESOURCES	As a nonprofit, Great Minds offers the <i>Eureka Math</i> curriculum as PDF downloads for free, noncommercial use. Access the free PDFs at greatminds.org/math/curriculum.		
	The teacher–writers who created the curriculum have also developed essential resources, available only from Great Minds, including the following: • Printed material in English and Spanish		
	<ul><li>Digital resources</li><li>Professional development</li></ul>		
	<ul> <li>Classroom tools and manipulatives</li> </ul>		
II	Teacher support materials		

• Parent resources

# New York State Next Generation Mathematics Learning Standards Correlation to *Eureka Math*™

### **GRADE K MATHEMATICS**

The majority of the Grade K New York State Next Generation Mathematics Learning Standards are fully covered by the Grade K *Eureka Math* curriculum. The areas where the Grade K New York State Next Generation Mathematics Learning Standards and Grade K *Eureka Math* do not align will require the use of *Eureka Math* content from other grade levels. A detailed analysis of alignment is provided in the table below.

### **INDICATORS**

Green indicates that the New York standard is fully addressed in *Eureka Math*.

Yellow indicates that the New York standard may not be completely addressed in *Eureka Math*.

Red indicates that the New York standard is not addressed in *Eureka Math*.

Blue indicates there is a discrepancy between the grade level at which this standard is addressed in the New York standards and in *Eureka Math*.

# 1: Make sense of problems and persevere in solving them.

Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

Lessons in every module engage students in making sense of problems and persevering in solving them as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 1, which is specifically addressed in the following modules:

GK M2: Two-Dimensional and Three-Dimensional Shapes GK M4: Number Pairs, Addition and Subtraction to 10 GK M6: Analyzing, Comparing, and Composing Shapes

#### **2:** Reason abstractly and quantitatively.

Mathematically proficient students make sense of quantities and their relationships in problem situations. They bring two complementary abilities to bear on problems involving quantitative relationships: the ability to *decontextualize*—to abstract a given situation and represent it symbolically and manipulate the representing symbols as if they have a life of their own, without necessarily attending to their referents and the ability to *contextualize*, to pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Quantitative reasoning entails habits of creating a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them; and knowing and flexibly using different properties of operations and objects. Lessons in every module engage students in reasoning abstractly and quantitatively as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 2, which is specifically addressed in the following modules:

GK M1: Numbers to 10

GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10

GK M4: Number Pairs, Addition and Subtraction to 10

GK M5: Numbers 10–20 and Counting to 100

# **3:** Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and-if there is a flaw in an argumentexplain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

Lessons in every module engage students in constructing viable arguments and critiquing the reasoning of others as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 3, which is specifically addressed in the following modules:

#### GK M1: Numbers to 10

GK M2: Two-Dimensional and Three-Dimensional Shapes

GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10

GK M5: Numbers 10–20 and Counting to 100

#### 4: Model with mathematics.

Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

Lessons in every module engage students in modeling with mathematics as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 4, which is specifically addressed in the following modules:

#### GK M1: Numbers to 10

GK M4: Number Pairs, Addition and Subtraction to 10

GK M5: Numbers 10–20 and Counting to 100

GK M6: Analyzing, Comparing, and Composing Shapes

#### 5: Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

Lessons in every module engage students in using appropriate tools strategically as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 5, which is specifically addressed in the following modules:

GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10

GK M4: Number Pairs, Addition and Subtraction to 10

#### 6: Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions. Lessons in every module engage students in attending to precision as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 6, which is specifically addressed in the following modules:

GK M2: Two-Dimensional and Three-Dimensional Shapes

GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10

GK M6: Analyzing, Comparing, and Composing Shapes

#### 7: Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see  $7 \times 8$  equals the well-remembered  $7 \times 5 + 7 \times 3$ , in preparation for learning about the distributive property. In the expression  $x^2 + 9x + 14$ , older students can see the 14 as  $2 \times 7$  and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see  $5-3(x-y)^2$  as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers *x* and *y*.

Lessons in every module engage students in looking for and making use of structure as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 7, which is specifically addressed in the following modules:

GK M1: Numbers to 10

GK M2: Two-Dimensional and Three-Dimensional Shapes

GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10

GK M4: Number Pairs, Addition and Subtraction to 10

GK M5: Numbers 10–20 and Counting to 100

GK M6: Analyzing, Comparing, and Composing Shapes

# 8: Look for and express regularity in repeated reasoning.

Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they repeatedly check whether points are on the line through (1, 2) with slope 3, middle school students might abstract the equation (y - 2)/(x - 1) = 3. Noticing the regularity in the way terms cancel when expanding  $(x - 1)(x + 1), (x - 1)(x^2 + x + 1), \text{ and } (x - 1)(x^3 + x^2 + x + 1)$  might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results. Lessons in every module engage students in looking for and expressing regularity in repeated reasoning as required by this standard. This practice standard is analogous to the CCSSM Standards for Mathematical Practice 8, which is specifically addressed in the following modules:

#### GK M1: Numbers to 10

GK M4: Number Pairs, Addition and Subtraction to 10

Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
Counting and	Cluster: Know number names and the count sequence.		
Cardinality	<b>NY-K.CC.1</b> Count to 100 by ones and by tens.	GK M5 Topic D: Extend the Say Ten and Regular Count Sequence to 100	
	<b>NY-K.CC.2</b> Count to 100 by ones beginning from any given number (instead of beginning at 1).	<ul> <li>GK M1 Topic G: One More with Numbers 0–10</li> <li>GK M5 Lesson 13: Show, count, and write to answer how many questions in linear and array configurations.</li> <li>GK M5 Topic D: Extend the Say Ten and Regular Count Sequence to 100</li> </ul>	
	NY-K.CC.3 Write numbers from 0 to 20. Represent a number of objects with a written numeral 0–20 (with 0 representing a count of no objects).	GK M1 Topic D: The Concept of Zero and Working with Numbers 0–5GK M1 Topic E: Working with Numbers 6–8 in Different ConfigurationsGK M1 Topic F: Working with Numbers 9–10 in Different ConfigurationsGK M5 Topic B: Compose Numbers 11–20 from 10 Ones and Some Ones; Represent and Write Teen NumbersGK M5 Lesson 14: Show, count, and write to answer how many questions with up to 20 objects in circular configurations.	

Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
	Cluster: Count to tell the number of objects.		
	<b>NY-K.CC.4</b> Understand the relationship between numbers and quantities up to 20; connect counting to cardinality.		
	a. When counting objects, say the number names in the standard order, pairing each object with one and only one number name and each number name with one and only one object. (1:1 correspondence)	GK M1: Numbers to 10 GK M6 Lesson 4: Describe the relative position of shapes using ordinal numbers.	
	b. Understand that the last number name said tells the number of objects counted, (cardinality). The number of objects is the same regardless of their arrangement or the order in which they were counted.	GK M1: Numbers to 10	

Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
	c. Understand the concept that each successive number name refers to a quantity that is one larger.	<ul> <li>GK M1 Topic G: One More with Numbers 0–10</li> <li>GK M3 Lesson 23: Reason to identify and make a set that has 1 more.</li> <li>GK M4 Lesson 37: Add or subtract 0 to get the same number and relate to word problems wherein the same quantity that joins a set, separates.</li> <li>GK M4 Lesson 38: Add 1 to numbers 1–9 to see the pattern of <i>the next number</i> using 5-group drawings and equations.</li> <li>GK M5 Topic A: Count 10 Ones and Some Ones</li> <li>GK M5 Topic C: Decompose Numbers 11–20, and Count to Answer "How Many?" Questions in Varied Configurations</li> </ul>
	d. Understand the concept of ordinal numbers (first through tenth) to describe the relative position and magnitude of whole numbers.	GK M6: Analyzing, Comparing, and Composing Shapes
	<b>NY-K.CC.5a</b> Answer counting questions using as many as 20 objects arranged in a line, a rectangular array, and a circle. Answer counting questions using as many as 10 objects in a scattered configuration.	GK M1: Numbers to 10 GK M5: Numbers 10–20 and Counting to 100
	<b>NY-K.CC.5b</b> Given a number from 1–20, count out that many objects.	GK M1: Numbers to 10 GK M5: Numbers 10–20 and Counting to 100

Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
	Cluster: Compare numbers.		
	<b>NY-K.CC.6</b> Identify whether the number of objects in one group is greater than (more than), less than (fewer than), or equal to (the same as) the number of objects in another group.	GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10	
	<b>NY-K.CC.7</b> Compare two numbers between 1 and 10 presented as written numerals.	GK M3 Topic F: Comparison of Sets Within 10 GK M3 Topic G: Comparison of Numerals	
Operations and Algebraic	Cluster: Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from.		
Thinking	<b>NY-K.OA.1</b> Represent addition and subtraction using objects, fingers, pennies, drawings, sounds, acting out situations, verbal explanations, expressions, equations or other strategies.	<ul><li>GK M1 Lesson 28: Act out <i>result unknown</i> story problems without equations.</li><li>GK M4: Number Pairs, Addition and Subtraction to 10</li></ul>	
	<b>NY-K.OA.2a</b> Add and subtract within 10.	GK M4: Number Pairs, Addition and Subtraction to 10	
	<b>NY-K.OA.2b</b> Solve addition and subtraction word problems within 10.	GK M4: Number Pairs, Addition and Subtraction to 10	

Domain	Standards for Mathematical Content	Aligned Components of Eureka Math
	NY-K.OA.3Decompose numbers less than or equal to 10 into pairs in more than one way.Record each decomposition with a drawing or equation.	<ul> <li>GK M1 Topic C: Numbers to 5 in Different Configurations, Math Drawings, and Expressions</li> <li>GK M1 Lesson 14: Write numerals 1–3. Represent decompositions with materials, drawings, and equations, 3 = 2 + 1 and 3 = 1 + 2.</li> <li>GK M1 Lesson 16: Write numerals 1–5 in order. Answer and make drawings of decompositions with totals of 4 and 5 without equations.</li> <li>GK M3 Lesson 7: Compare objects using <i>the same as</i>.</li> <li>GK M4: Number Pairs, Addition and Subtraction to 10</li> </ul>
	NY-K.OA.4 Find the number that makes 10 when given a number from 1 to 9. Record the answer with a drawing or equation.	<ul> <li>GK M4 Lesson 39: Find the number that makes 10 for numbers 1–9, and record each with a 5-group drawing.</li> <li>GK M4 Lesson 40: Find the number that makes 10 for numbers 1–9, and record each with an addition equation.</li> <li>GK M5 Lesson 10: Build a Rekenrek to 20.</li> </ul>
	<b>NY-K.OA.5</b> Fluently add and subtract within 5.	GK M4 Topic A: Compositions and Decompositions of 2, 3, 4, and 5
	Cluster: Understand simple patterns.	
	<b>NY-K.OA.6</b> Duplicate, extend, and create simple patterns using concrete objects.	GPK M5 Topic F: Duplicating and Extending Patterns

Domain	Standards for Mathematical Content		Aligned Components of Eureka Math	
Numbers and	Cluster: Work with numbers 11–19 to gain foundations for place value.			
Operations in Base Ten	<b>NY-K.NBT.1</b> Compose and decompose the numbers from 11 to 19 into ten ones and one, two, three, four, five, six, seven, eight, or nine ones.		GK M5: Numbers 10–20 and Counting to 100	
Measurement	Cluster: Describe and compare measurab	le a	attributes.	
and Data	<b>NY-K.MD.1</b> Describe measurable attributes of an object(s), such as length or weight, using appropriate vocabulary.		GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10	
	<b>NY-K.MD.2</b> Directly compare two objects with a common measurable attribute and describe the difference.		GK M3: Comparison of Length, Weight, Capacity, and Numbers to 10	
	Cluster: Classify objects and count the number of objects in each category.			
	NY-K.MD.3		GK M1 Topic A: Attributes of Two Related Objects	
	Classify objects into given categories; count the objects in each category and sort the categories by count.		GK M1 Topic B: Classify to Make Categories and Count	
	by count.		GK M2 Topic C: Two-Dimensional and Three-Dimensional Shapes	
	<b>NY-K.MD.4</b> Explore coins (pennies, nickels, dimes, and quarters) and begin identifying pennies and dimes.		G1 M6 Topic E: Coins and Their Values	

Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
Geometry	Cluster: Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres).		
	<b>NY-K.G.1</b> Describe objects in the environment using names of shapes, and describe the relative positions of these objects using terms such as above, below, beside, in front of, behind, and next to.	<ul> <li>GK M2 Lesson 5: Describe and communicate positions of all flat shapes using the words <i>above</i>, <i>below</i>, <i>beside</i>, <i>in front of</i>, <i>next to</i>, and <i>behind</i>.</li> <li>GK M2 Lesson 8: Describe and communicate positions of all solid shapes using the words <i>above</i>, <i>below</i>, <i>beside</i>, <i>in front of</i>, <i>next to</i>, and <i>behind</i>.</li> </ul>	
	<b>NY-K.G.2</b> Name shapes regardless of their orientation or overall size.	GK M2: Two-Dimensional and Three-Dimensional Shapes	
	<b>NY-K.G.3</b> Understand the difference between two- dimensional (lying in a plane, "flat") and three- dimensional ("solid") shapes.	GK M2 Topic C: Two-Dimensional and Three-Dimensional Shapes	

Domain	Standards for Mathematical Content	Aligned Components of Eureka Math	
	Cluster: Analyze, compare, sort, and compose shapes.		
	NY-K.G.4	GK M2: Two-Dimensional and Three-Dimensional Shapes	
	Analyze, compare, and sort two- and three- dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts, and other attributes.	GK M6: Analyzing, Comparing, and Composing Shapes	
	<b>NY-K.G.5</b> Model objects in their environment by building and/or drawing shapes.	GK M6: Analyzing, Comparing, and Composing Shapes	
	<b>NY-K.G.6</b> Compose larger shapes from simple shapes.	GK M6: Analyzing, Comparing, and Composing Shapes	